

# **Electricity**

### **ANSWERS**

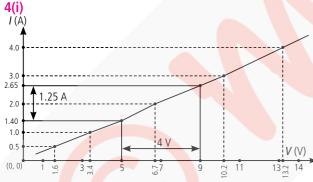
- **1.** A heater coil should have (i) high resistivity and (ii) high melting point.
- **2.** The cells are connected in series, to get maximum voltage.
- **3(i)** The S.I. unit of electric power is watt (W).
- **3(ii)** Kilowatt hour is the unit of electrical energy.

3(iii) Current, 
$$I = \frac{P}{V} = \frac{P}{RI}$$

$$I^2 = \frac{P}{R} = \frac{1}{10000}$$

$$I = \frac{1}{100} = 0.01 \,\text{A}$$

**3(iv)** The power rating of an electrical appliance is the electrical energy consumed per second by the appliance when connected across the marked voltage of the mains.



**4(ii)** For V = 4 V (*i.e.*, 9 V - 5 V)

 $I = 1.25 \,\mathrm{A} \,(i.e., 2.65 \,\mathrm{A} - 1.40 \,\mathrm{A})$ 

Therefore,  $R = \frac{V}{I} = \frac{4 \text{ V}}{1.25 \text{ A}} = 3.2 \Omega$ 

The value of R obtained from the graph depends upon the accuracy with which the graph is plotted.

- **4(iii) (a) :** Nature of *V-I* graph is a straight line passing through the origin of the graph.
- **4(iv) (b) :** The slope of *V-I* graph gives the value of the resistance of the conductor at the given temperature.
- **5. (c)**: Fuse wire does not depend on its length.

OR

(a): Nichrome is one of best heating element.

- **6. (a)**: The smallest resistance can be obtained by combining those resistance in parallel. Thus, here smallest resistance is R/n.
- **7. (a)** : Resistance is inversely proportional to power of the bulb.

$$P \propto V^2/R$$

**8. (c)**: Ammeter is always connected in series and voltmeter in parallel with the resistor.

OF

(c): To apply a variable resistance in the circuit.

9. **(b)**: 
$$V_1 = IR_1 = 10 \times 2 = 20 \text{ V}$$
,

$$V_2 = IR_2 = 10 \times 4 = 40 \text{ V},$$

$$V_3 = 10 \times 6 = 60 \text{ V}.$$

**10. (c)**: Resistance is directly proportional to length and inversely proportional to square of diameter.

OR

(c) : The resistors will be 3  $\Omega$  and 6  $\Omega$ .  $R_s=3+6=9$   $\Omega$ 

and 
$$R_p = \frac{3 \times 6}{3 + 6} = 2\Omega$$
.

**11. (b)**: As we know, V = IR from Ohm's law. So, if resistance is doubled, then current becomes half.

**12.** (a) : 
$$R = \rho \frac{I}{A}$$

$$R_A: R_B = [(5 \times 4)/(2)^2]: [(18 \times 9)/(3)^2] = 5:18.$$

**13. (c)** : Assertion is true but reason is false.

 $1 \text{ kWh} = 1 \text{ kW} \times 1 \text{ hour}$ 

$$= 1000 (joule/s) \times 3600 s$$

$$= 36 \times 10^5$$
 joule

- *i.e.*, kWh is the unit of electric energy and used for expressing consumed electric energy.
- **14. (b)**: Both the assertion and reason are true but reason is not the correct explanation of assertion.

The resistance,  $R = \frac{V^2}{P}$ , i.e.,  $R \propto 1/P$ 

- *i.e.*, higher is the wattage of a bulb, lesser is the resistance and so it will glow brighter.
- **15.** (a) Bulbs  $B_1$ ,  $B_2$  and  $B_3$  are connected in parallel, so potential difference across each is same. When bulb  $B_1$  gets fused, potential difference across  $B_2$  and  $B_3$  does not change, so, their glow remains unchanged.

**(b)** Let the resistance of each bulb be R  $\Omega$ , then net resistance of the circuit,

$$\frac{1}{R_P} = \frac{1}{R} + \frac{1}{R} + \frac{1}{R} = \frac{3}{R} \text{ or } R_P = \frac{R}{3} \Omega$$

Now, I = 3 A, V = 4.5 V

$$\therefore$$
  $R_P = \frac{V}{I}$  or  $\frac{R}{3} = \frac{4.5}{3}$  or  $R = 4.5 \Omega$ 

When bulb  $B_2$  gets fused, no current flows through ammeter  $A_2$ .

:. Resistance of the circuit.

$$\frac{1}{R_{\text{new}}} = \frac{1}{R} + \frac{1}{R} = \frac{2}{R} \quad \text{or} \quad R_{\text{new}} = \frac{R}{2} = \frac{4.5}{2} \Omega$$
  
 $\therefore I_{\text{new}} = \frac{V}{R_{\text{new}}} = \frac{4.5 \times 2}{4.5} = 2 \text{ A}$ 

This current divides equally in bulb  $B_1$  and  $B_3$ .

Therefore reading of  $A_1$ ,  $A_2$ ,  $A_3$  and A are 1 A, 0, 1 A and 2 A respectively.

- (c) When all the three bulbs glow, I = 3 A, V = 4.5 V
- $\therefore$  Power dissipated in the circuit, P = VI

$$= 3 A \times 4.5 V = 13.5 W$$

**16.** The slope of the line in *V-I* graph, is  $\frac{V}{I} = R$ 

We know that resistance in series is greater than the resistance in parallel. The graph shows series resistance have greater slope and is therefore, correct.

In graph (b), the slope of the line is  $\frac{l}{V} = \frac{1}{R}$  *i.e.*, the reciprocal. So, only graph (a) is correctly labelled.

$$R_{A} = \rho \frac{l}{\pi r^{2}}; R_{B} = \rho \frac{2l}{\pi (2r)^{2}} = \rho \frac{l}{2\pi r^{2}}$$

$$\frac{1}{R_{P}} = \frac{1}{R_{A}} + \frac{1}{R_{B}} = \frac{\pi r^{2}}{\rho l} + \frac{2\pi r^{2}}{\rho l} = \frac{3\pi r^{2}}{\rho l}$$

$$\therefore R_{P} = \frac{\rho l}{3\pi r^{2}}$$
Now, 
$$\frac{R_{P}}{R_{A}} = \frac{\rho l / 3\pi r^{2}}{\rho l / \pi r^{2}} = \frac{\rho l}{3\pi r^{2}} \times \frac{\pi r^{2}}{\rho l} = \frac{1}{3}$$

( $\rho$  is same for both resistors A and B because both are of same metal.)

**17.** For the same potential difference, the power and resistance of different appliances are related as  $P \propto \frac{1}{R}$ . This means higher the resistance, lesser will be the power of the appliance.

If a same amount of current is passing through different appliances then power of an appliance is related to the resistance as  $P \propto R$ , *i.e.*, higher the resistance, more is the power of appliance.

#### OR

In this case we have been given power P and voltage V, so the current will be :

$$P = V \times I$$

Here, power, P = 40 watts

voltage, V = 220 volts

and, current, I = ?

(To be calculated)

Now, putting these values in the above formula, we get :

$$40 = 220 \times I$$

$$I = \frac{40}{220} = \frac{2}{11}$$

Thus, current, I = 0.18 ampere

**18.** Potential difference, V = 24 volts

Resistance, R = 120 ohms

and Current, I = ?

Now, putting these values in the Ohm's law we get,

$$\frac{V}{I} = R$$
 or  $\frac{24}{I} = 120$   
o,  $120I = 24$ 

$$\Rightarrow I = \frac{24}{120}$$
 ampere

I = 0.2 ampere (or 0.2 A)

Thus, the current flowing in the circuit is 0.2 ampere.

**19.** First of all we will calculate the resistance of electric heater. Now, in the first case, the electric heater draws a current of 3.4 A from 220 V supply line. So,

potential difference, V = 220 V

Current, I = 4 A and resistance, R = ?

Now, 
$$\frac{V}{I} = R$$

 $\therefore$  Resistance, R = 55 W

Thus, the resistance of electric heater is 55 ohms. This resistance will now be used to find out the current drawn when the electric heater is connected to 110 V supply line. So,

$$\frac{V}{I} = R \implies \frac{110}{I} = 55$$

.. Current, 
$$I = \frac{110}{55} = 2 \text{ A}$$

**20.** If only resistors are connected to the battery, the source energy continually gets dissipated entirely in the form of heat. This is known as heating effect of current. The amount of heat (*H*) produced in time *t* is given by Joule's law of heating.

$$H = I^2Rt$$

Where, *I* is current flowing through resistor *R* for time *t*.

The electric laundry iron, electric toaster, electric oven, electric kettle and electric heater are some common devices based on heating effect of current.

OR

Here, P = 750 W, V = 200 V

- (a) As P = VII = P/V = (750/200) A = 3.75A
- **(b)** By Ohm's law V = IR or R = V/I

$$\therefore R = \frac{200}{3.75} \Omega = 53.3 \Omega$$

(c) Energy consumed by the iron in 2 hours

$$= P \times t = 750 \text{ W} \times 2\text{h} = 1.5 \text{ kWh}$$

or 
$$E = (750 \times 2 \times 3600) \text{ J} = 5.4 \times 10^6 \text{ J}$$

**21.** Suppose the length of 12  $\Omega$  resistance wire is *I*, its area of cross-section is *A* and its resistivity is  $\rho$ . Then:

$$R = \frac{\rho \times l}{A}$$
 or  $12 = \frac{\rho \times l}{A}$  ...(i

Now, when this wire is doubled up by folding, then its length will becomes half, that is, the length will become  $\frac{l}{2}$ . But on doubling the wire by folding, its area of cross-section will become double, that is, the area of cross-section will becomes 2 A. Suppose the new resistance of the doubled up wire (or folded wire) is R, So,

$$R = \frac{\rho \times l}{2 \times 2 A}$$
 or  $R = \frac{\rho \times l}{4 A}$  ...(ii)

Now, dividing equation (ii) by equation (i), we get:

$$\frac{R}{12} = \frac{\rho \times l \times A}{4A \times \rho \times l} \quad \text{or} \quad \frac{R}{12} = \frac{1}{4}$$

$$4R = 12 \Rightarrow R = \frac{12}{4} \Rightarrow R = 3 \Omega$$

22. We know that, electrical energy =  $Power \times time$ 

or 
$$E = P \times t$$
 ...(i)

We want to calculate the electrical energy in kilowatthours, so first we should convert the power of 120 watts into kilowatts by dividing it by 1000. That is power, P = 120 watts

$$= \frac{120}{1000} \text{kilowatt} = 0.12 \text{ kilowatt}$$

and, time, t = 50 hours

Now, putting P = 0.12 kW and t = 50 hours in equation (i), we get:

Electrical energy,  $E = 0.12 \times 50 = 6$  kilowatt-hours

Thus, electrical energy consumed is 6 kilowatt-hours.

**23.** (a) The current can be calculated by using Ohm's law:

$$\frac{V}{I} = F$$

Here, potential difference, V = 220 volts

current, I = ?

resistance, R = 11000 ohms

Putting these values in the above formula, we get:

$$\frac{220}{I} = 11000$$

So, 
$$I = \frac{220}{11000} = 0.02 \text{ A}$$

Thus, the current flowing in the electric iron is 0.02 A.

**(b)** The heat energy in joules can be calculated by using the Joule's law heating

$$H = I^2 \times R \times t$$

Here, current, I = 0.02 A

resistance, 
$$R = 11000 \Omega$$

and time, t = 10 s

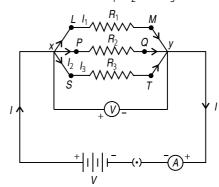
Putting these values in the above formula, we get

$$H = (0.02)^2 \times 11000 \times 10 = 44 \text{ J}.$$

**24.** Since electric heater has more power than an electric bulb and power is reciprocal to resistance for a given supply voltage (*i.e.*,  $P \propto 1/R$ ), therefore, the resistance of heater coil is less than that of electric bulb.

When the heater, which is connected in parallel with the illuminating bulb is switched on, it draws more current from the current supplied. Due to it, the bulb becomes dim, as current through bulb decreases. After sometime, the heater coil becomes hot. Its resistance increases. Current through heater coil decreases and in turn current through the lamp increases. Also, the supply of current increases to maintain the required voltage. Due to it, the dimness of the bulb decreases.

**25.** The following circuit diagram depicts the parallel connection of three resistors  $R_1$ ,  $R_2$  and  $R_3$ .



Let currents  $I_1$ ,  $I_2$  and  $I_3$  flow through the resistors  $R_1$ ,  $R_2$  and  $R_3$  respectively.

It is observed that total current *I* is equal to the sum of the separate currents through each branch.

So, 
$$I = I_1 + I_2 + I_3$$
 ...(i)

Let  $R_P$  be the equivalent resistance. Then,

$$I = \frac{V}{R_P}$$

On applying Ohm's law to each resistor,

$$I_1 = \frac{V}{R_1}, \ I_2 = \frac{V}{R_2}, \ I_3 = \frac{V}{R_3}$$

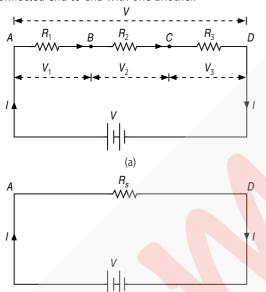
From equation (i), we have

$$\frac{V}{R_P} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$
 or  $\frac{1}{R_P} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$ 

Voltmeter is connected in parallel across the resistor whose potential difference is to measure and ammeter is connected in series with resistor in the circuit.

#### OF

**(a)** Resistors are said to be connected in series, if the same current is flowing through each resistor when some potential difference is applied across the combination. Here the resistors are connected end to end with one another.



In figure three resistance wires AB, BC and CD are connected in series. Suppose their resistances are respectively  $R_1$ ,  $R_2$  and  $R_3$ . Let the equivalent resistance of these resistances be  $R_5$ . Suppose a current I is flowing in all the three resistances. Suppose the potential differences between the ends of the resistances  $R_1$ ,  $R_2$  and  $R_3$  are respectively  $V_1$ ,  $V_2$  and  $V_3$ .

(b)

$$\therefore V_1 = IR_1, V_2 = IR_2 \text{ and } V_3 = IR_3.$$

If the potential difference between A and D be V, then

$$V = V_1 + V_2 + V_3$$
  
=  $IR_1 + IR_2 + IR_3$   
=  $(R_1 + R_2 + R_3)I$  ...(i)

The equivalent resistance between A and D is  $R_s$ . Therefore,

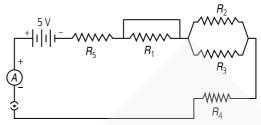
$$V = IR_s$$
 ...(ii)

Comparing eq. (i) and (ii), we get

$$IR_s = I(R_1 + R_2 + R_3)$$

or 
$$R_s = R_1 + R_2 + R_3$$

**(b)** Given circuit can be redrawn as follows:



- (i) Resistors,  $R_5$  and  $R_4$  are connected in series.
- (ii) Resistors,  $R_2$  and  $R_3$  are connected in parallel.
- (iii)  $R_1$  is shorted, hence it will not contribute to the circuit. Equivalent resistance of  $R_2$  and  $R_3$  will be

$$\frac{1}{R'} = \frac{1}{R_2} + \frac{1}{R_3} = \frac{1}{2} + \frac{1}{2}$$

$$\frac{1}{R'} = \frac{1}{1} \quad \text{or} \quad R' = 1 \ \Omega$$

Then R' is connected in series with  $R_4$  and  $R_5$ .

So, equivalent resistance of the circuit is

$$R_{\text{eq}} = R' + R_4 + R_5 = 1 + 2 + 2 = 5 \Omega$$

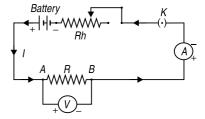
Using Ohm's law, 
$$I = \frac{V}{R_{eq}} = \frac{5}{5} = 1 \text{ A}$$

So, total current flowing in the circuit will be 1 A.

**26.** Ohm's law states that the electric current flowing through a metallic wire is directly proportional to the potential difference *V*, across its ends provided its temperature remains the same.

$$V \propto I$$
 or  $\frac{V}{I} = \text{constant} = R$   
or  $V = IR$ 

To experimentally verify Ohm's law, an electric circuit as shown in figure is set up which contains the following components.



- (i) A battery which is used to send current in the circuit.
- (ii) A rheostat (*Rh*) which is a variable resistance and is used to change and adjust current in the circuit.
- (iii) A resistance wire AB of fixed resistance R.
- (iv) An ammeter (A) which is used to measure current in the circuit (i.e., current through R.) It is connected in series with the resistance R so that the current through A is the same as that passing through R. Also note that the +ve terminal of A is connected to positive terminal of the battery and its -ve terminal is connected to the negative terminal of the battery.

- (v) A voltmeter (V) is connected in parallel across R to measure potential difference between the point A and B of the resistance wire. Again, note that the +ve terminal of V goes to positive terminal of the battery and the -ve terminal goes to negative terminal of the battery.
- (vi) A plug key, K is used to open or close the circuit as and when required.

When the key K is closed, a current starts flowing in the circuit. The current in the circuit is changed by adjusting the rheostat and the readings of V and A are taken. These readings give us the values of potential difference (V) across R and the current (I) flowing through it.

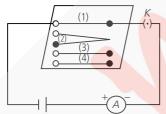
It is found that V/I is practically constant, i.e.,  $\frac{V}{I}$  = constant or  $V \propto I$ . This verifies Ohm's law.

Ohm's law does not hold good under all conditions. It is obeyed by metallic conductors only when physical conditions like temperature etc. remain unchanged.

#### OR

Resistivity is numerically equal to the resistance of a wire of unit length having a unit area of cross-section. Its SI unit is ohm-metre ( $\Omega$  m).

Make an electric circuit consisting of a cell, an ammeter, a nichrome wire of length I [say, marked (1)] and a plug key, as shown in figure.



- (i) Now, plug the key. Note the current in the ammeter.
- (ii) Replace the nichrome wire by another nichrome wire of same thickness but twice the length, that is 2*I* [marked (2)] in the figure.
- (iii) Note the ammeter reading.
- (iv) Now replace the wire by a thicker nichrome wire, of the same length / [marked (3)]. A thicker wire has a larger cross-sectional area. Again note down the current through the circuit.
- (v) Instead of taking a nichrome wire, connect a copper wire [marked (4) in figure] in the circuit. Let the wire be of the same length and same area of cross-section as that of the first nichrome wire [marked (1)]. Note the value of the current.
- (vi) Notice the difference in the current in all cases.

It is observed that the ammeter reading decreases to one-half when the length of the wire is doubled. The ammeter reading is increased when a thicker wire of the same material and of the same length is used in the circuit. A change in ammeter reading is observed when a wire of different material of the same length and the same area of cross-section is used. On applying Ohm's law, we observe that the resistance of the conductor depends (i) on its length, (ii) on its area of cross-section, and (iii) on the nature of its material.

- **27.** (a) When the bulbs are in series, current I = constant. As  $P = I^2 R$ , so  $P \propto R$ . Hence, the lamp with higher resistance (i.e.,  $R_1$ ) will glow more brightly.
- **(b)** When the two bulbs are operating in series, total illumination,  $P = \frac{V^2}{(R_1 + R_2)}$ .

When the lamp of resistance  $R_2$  gets burned and bulb of resistance  $R_1$  alone is operated, then illumination,  $P' = \frac{V^2}{R_1}$ , i.e., P' > P.

So, the net illumination will increase.

(c) When the bulbs are in parallel, voltage across each bulb

is same, as, 
$$P = \frac{V^2}{R}$$
, so  $P \propto \frac{1}{R}$ .

Hence, the lamp with lower resistance (i.e.,  $R_2$ ) will glow brightly.

(d) When both the bulbs are operating in parallel, then total

illumination, 
$$P = P_1 + P_2 = \frac{V^2}{R_1} + \frac{V^2}{R_2}$$

When lamp of resistance  $R_1$  burns out, only lamp of resistance  $R_2$  will give light. Then illumination is

$$P' = \frac{V^2}{R_2}$$
, i.e.,  $P' < P$ .

So, the net illumination will decrease.

OR

In the first case:

Power, P = 1000 W

Potential difference, V = 220 V

And, resistance, R = ?

Now, 
$$P = \frac{V^2}{R}$$

So, 
$$1000 = \frac{(220)^2}{R}$$

and 
$$R = \frac{220 \times 220}{1000} = 48.4 \Omega$$

This resistance of 48.4  $\Omega$  of the bulb will remain unchanged. In the second case :

Power, P = ?

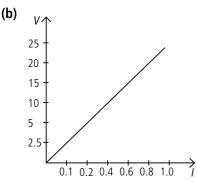
Potential difference, V = 110 V

And, resistance,  $R = 48.4 \Omega$ 

Now, 
$$P = \frac{V^2}{R}$$
  

$$\therefore P = \frac{(110)^2}{48.4} = \frac{110 \times 110}{48.4} = 250 \text{ W}$$

**28. (a)** Ratio of potential difference and current is known as resistance.



Resistance, 
$$R = \frac{\Delta V}{\Delta I} = \frac{20 - 10}{0.8 - 0.4} = \frac{10}{0.4} = 25 \,\Omega$$

- (c) Ohm's law is illustrated by *V–I* graph.
- **(d)** The formula which states relation between potential difference, current and resistance is, V = IR.
- (e) Potential difference between terminals of an electric iron, V = 240 V and current, I = 5 A

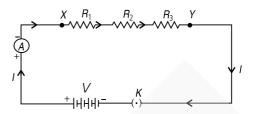
∴ Resistance of the electric iron, 
$$R = \frac{V}{I} = \frac{240}{5} = 48 \Omega$$

**29.** Join three resistors of different values in series. Connect them with a battery, an ammeter and a plug key, as shown in figure. We may use the resistors  $R_1$ ,  $R_2$ ,  $R_3$  etc., and a battery of potential difference V for performing this activity.

Plug the key. Note the ammeter reading.

Change the position of ammeter to anywhere in between the resistors. Note the ammeter reading each time.

It is observed that the value of the current in the ammeter is the same, independent of its position in the electric circuit. It means that in a series combination of resistors, the current is the same in every part of the circuit or the same current through each resistor.



**30.** Here we know the voltage and power of the bulb. So, resistance can be calculated by using,

$$P = \frac{V^2}{R}$$

Here, power, P = 100 watts

voltage, V = 220 volts

and, resistance, R = ?

Now, putting these values in the above formula, we get:

$$100 = \frac{(220)^2}{R} \Rightarrow 100 R = 48400$$

$$\Rightarrow R = \frac{48400}{100} = 484 \text{ ohms}$$

The electrical energy consumed in kilowatt-hours can be calculated by using,

$$E = P \times t$$

Here, power, P = 100 watts

$$= \frac{100}{1000} \text{ kilowatt} = 0.1 \text{ kilowatt} \qquad \dots (1)$$

and time, 
$$t = 7$$
 hours ...(2)

So, energy consumed by 1 bulb =  $0.1 \times 7$ 

= 0.7 kilowatt-hours

And, energy consumed by 5 bulbs =  $0.7 \times 5$ 

= 3.5 kilowatt-hours (or 3.5 kWh)

Thus, the total electrical energy consumed is "3.5 kilowatthours" or "3.5 units".

We have been given that:

Cost of 1 unit of electricity = ₹ 2.30

So, cost of 2 units of electricity =  $\mathbf{\xi}$  2.30  $\times$  3.5 =  $\mathbf{\xi}$  8.05

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