

Some Applications of Trigonometry

EXAM DRILL

SOLUTIONS

1. (d) : Let A be the kite and AC is the string.

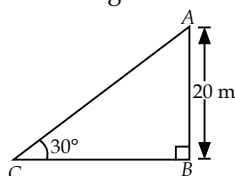
In right $\triangle ABC$, we have

$$\sin 30^\circ = \frac{BA}{AC}$$

$$\Rightarrow \frac{1}{2} = \frac{20}{AC}$$

$$\Rightarrow AC = 40 \text{ m}$$

Hence, the length of the string is 40 m.

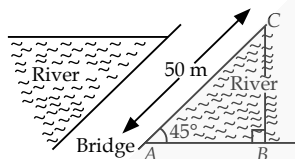


2. (c) : From figure, in right $\triangle ABC$, we have

$$\sin 45^\circ = \frac{BC}{AC}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{BC}{50}$$

$$\Rightarrow BC = \frac{50}{\sqrt{2}} = 25\sqrt{2} \text{ m}$$



Hence, the width of the river is $25\sqrt{2}$ m.

3. (a) : Let $\angle ACB = \theta$

In right $\triangle ABC$,

$$\tan \theta = \frac{AB}{BC} = \frac{4}{4\sqrt{3}} \Rightarrow \tan \theta = \frac{1}{\sqrt{3}} = \tan 30^\circ \Rightarrow \theta = 30^\circ$$

Now, $\angle ACB = \angle CAD = 30^\circ$ [Alternate angles]

Hence, angle of depression from A is 30° .

4. (b) : Let AB and CD are two poles of height 14 m and 20 m respectively. AD is the wire.

$$\text{Now, } DE = CD - CE$$

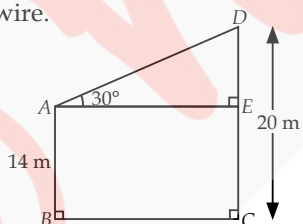
$$= 20 - 14 = 6 \text{ m}$$

In right $\triangle ADE$,

$$\tan 30^\circ = \frac{DE}{AE}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{6}{AE} \Rightarrow AE = 6\sqrt{3} \text{ m}$$

Hence, distance between two poles is $6\sqrt{3}$ m.



5. Let $AC = h$ m be the height of the pole.

Length of the shadow = $BC = 5\sqrt{3}$ m

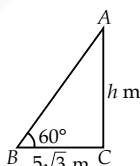
It is given that the sun's elevation is 60° .

$$\therefore \angle B = 60^\circ$$

In right $\triangle ACB$, we have

$$\frac{AC}{BC} = \tan 60^\circ \Rightarrow \frac{h}{5\sqrt{3}} = \sqrt{3} \Rightarrow h = 15$$

Hence, the height of the pole is 15 m.

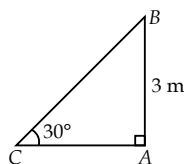


6. Let BC be the length of ramp and AC be the horizontal path.

$AB = 3$ m and $\angle ACB = 30^\circ$

In right $\triangle ABC$,

$$\sin 30^\circ = \frac{AB}{BC} \Rightarrow \frac{1}{2} = \frac{3}{BC} \Rightarrow BC = 6 \text{ m}$$



7. $AB = 6$ m, $AD = 2.54$ m (given)

$$\therefore BD = AB - AD = 6 - 2.54 = 3.46 \text{ m}$$

Hence, in $\triangle BDC$,

$$\frac{BD}{CD} = \sin 60^\circ \Rightarrow \frac{3.46}{CD} = \frac{\sqrt{3}}{2} \Rightarrow CD = 4 \text{ m}$$

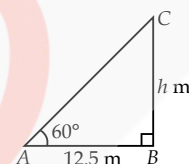
8. Let the height of the tower be h m.

In right $\triangle ABC$,

$$\tan 60^\circ = \frac{BC}{AB} = \frac{h}{12.5}$$

$$\Rightarrow \sqrt{3} = h/12.5 \Rightarrow h = 12.5\sqrt{3}$$

\therefore Height of the tower is $12.5\sqrt{3}$ m.



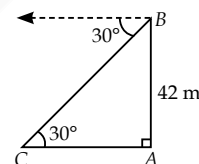
9. Let B be the position of the observer on the bridge and C be the position of boat.

Now, in right $\triangle ABC$,

$$\tan 30^\circ = \frac{AB}{AC}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{42}{AC} \Rightarrow AC = 42\sqrt{3} \text{ m}$$

\therefore Required distance is $42\sqrt{3}$ m.

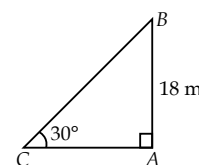


10. Let AB is the pillar of height 18 m and AC is the shadow of AB .

In right $\triangle ABC$, $\tan 30^\circ = \frac{AB}{AC}$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{18}{AC} \Rightarrow AC = 18\sqrt{3} \text{ m}$$

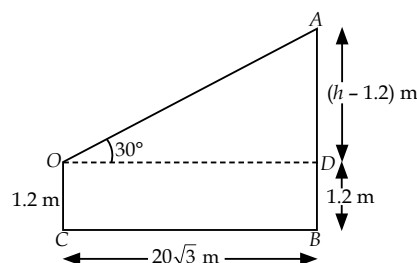
\therefore Required length of shadow is $18\sqrt{3}$ m.



11. Let CO be the observer, who is 1.2 m tall.

Let AB be the tower of height h m and $CB = 20\sqrt{3}$ m.

Let O be the point of observation of the angle of elevation of the top of tower such that $\angle AOD = 30^\circ$.



Draw OD parallel to CB such that $OD = CB = 20\sqrt{3}$ m.

In right $\triangle AOD$, we have

$$\tan 30^\circ = \frac{AD}{OD} \Rightarrow \frac{1}{\sqrt{3}} = \frac{h - 1.2}{20\sqrt{3}}$$

$$\Rightarrow h - 1.2 = 20 \Rightarrow h = 21.2$$

Hence, the height of the tower is 21.2 m.

12. Let AB be the tower and AC and AD are the shadows of tower AB , such that $AC + 14 = AD$

In right $\triangle ABC$,

$$\tan 45^\circ = \frac{AB}{AC}$$

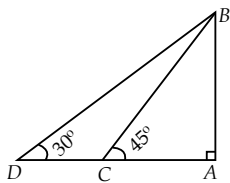
$$\Rightarrow 1 = \frac{AB}{AC} \Rightarrow AB = AC \quad \dots(i)$$

In right $\triangle ABD$,

$$\tan 30^\circ = \frac{AB}{AD} \Rightarrow \frac{1}{\sqrt{3}} = \frac{AB}{AC+14} \Rightarrow AC+14 = AB\sqrt{3}$$

$$\Rightarrow AB\sqrt{3} - AB = 14 \quad [\text{From (i)}]$$

$$\Rightarrow AB = \frac{14}{\sqrt{3}-1} \times \frac{\sqrt{3}+1}{\sqrt{3}+1} = 7(\sqrt{3}-1) = 5.124 \text{ m}$$



13. Let AB be the lamp-post and CD be the boy after walking 5 seconds. Let $DE = x$ m be the length of his shadow such that $BD = 1.5 \times 5 = 7.5$ m.

Let $\angle AEB = \angle CED = \theta$

Now, in right $\triangle CED$,

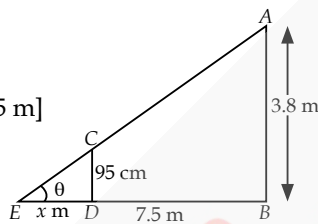
$$\tan \theta = \frac{CD}{ED} = \frac{0.95}{x} \quad \dots(i)$$

$$[\because CD = 95 \text{ cm} = 0.95 \text{ m}]$$

In right $\triangle ABE$,

$$\tan \theta = \frac{AB}{ED}$$

$$\Rightarrow \tan \theta = \frac{3.8}{7.5+x} \quad \dots(ii)$$



From (i) and (ii), we get

$$\frac{0.95}{x} = \frac{3.8}{7.5+x}$$

$$\Rightarrow 7.5 \times 0.95 + 0.95x = 3.8x \Rightarrow 7.125 + 0.95x = 3.8x$$

$$\Rightarrow 7.125 = 3.8x - 0.95x \Rightarrow 7.125 = 2.85x \Rightarrow x = 2.5$$

Hence, the length of his shadow after 5 seconds is 2.5 m.

14. Let A be the point on the ground which is 70 m away from the tower. Let BC be the tower of height h m and CD the flagstaff of height x m.

It is given that the angle of elevation of the top of the flagstaff from the point A is 60° and angle of elevation of the bottom of the flagstaff from the point A is 45° .

$\therefore \angle CAB = 45^\circ$ and $\angle DAB = 60^\circ$

In right $\triangle CBA$,

$$\tan 45^\circ = \frac{BC}{AB} \Rightarrow 1 = \frac{h}{70} \quad \dots(i)$$

Now, in right $\triangle DBA$,

$$\tan 60^\circ = \frac{DB}{AB}$$

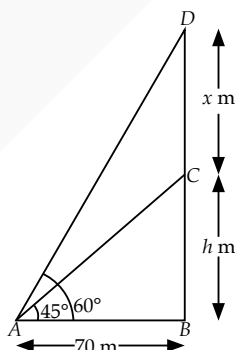
$$\Rightarrow \sqrt{3} = \frac{h+x}{70}$$

$$\Rightarrow \sqrt{3} = \frac{70+x}{70} \quad [\text{Using (i)}]$$

$$\Rightarrow 70\sqrt{3} = 70 + x \Rightarrow x = 70\sqrt{3} - 70$$

$$\Rightarrow x = 70(\sqrt{3} - 1) \Rightarrow x = 70(0.732) \Rightarrow x = 51.24$$

Hence, the height of the flagstaff is 51.24 m and the height of the tower is 70 m.



15. Let A be the first aeroplane, vertically above another aeroplane B such that $AC = 5000$ m be the height of the first aeroplane from the ground.

Let O be a point on the ground such that $\angle AOC = 60^\circ$ and $\angle BOC = 45^\circ$.

In right $\triangle AOC$,

$$\tan 60^\circ = \frac{AC}{OC}$$

$$\Rightarrow \sqrt{3} = \frac{AC}{OC}$$

$$\Rightarrow OC = \frac{5000}{\sqrt{3}} \quad [\because AC = 5000 \text{ m}]$$

$$\Rightarrow OC = \frac{5000\sqrt{3}}{3} = 2883.3 \text{ m} \quad \dots(i)$$

In right $\triangle BOC$,

$$\tan 45^\circ = \frac{BC}{OC} \Rightarrow 1 = \frac{BC}{OC} \Rightarrow BC = OC$$

$$\Rightarrow BC = 2883.3 \text{ m}$$

[Using (i)]

Thus, $AB = AC - BC$

$$= 5000 - 2883.3 = 2116.7 \text{ m}$$

$\dots(ii)$

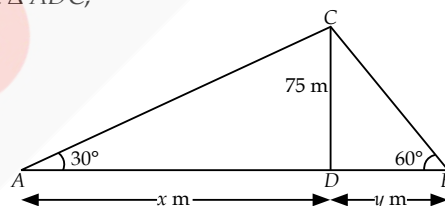
Hence, the vertical distance between the two aeroplanes is 2116.7 m.

16. Let $CD = 75$ m be the height of the building. Let A and B be the points of observations such that the angle of elevation at A is 30° and the angle of elevation at B is 60° .

$\therefore \angle CAD = 30^\circ$ and $\angle CBD = 60^\circ$

Let $AD = x$ m and $DB = y$ m.

In right $\triangle ADC$,



$$\tan 30^\circ = \frac{CD}{AD} \Rightarrow \frac{1}{\sqrt{3}} = \frac{75}{x} \Rightarrow x = 75\sqrt{3} \text{ m} \quad \dots(i)$$

In right $\triangle BDC$,

$$\tan 60^\circ = \frac{CD}{DB} \Rightarrow \sqrt{3} = \frac{75}{y} \Rightarrow y = \frac{75}{\sqrt{3}} \text{ m} \quad \dots(ii)$$

The distance between two men is AB , i.e.,

$$AB = AD + DB = x + y$$

$$\Rightarrow AB = \left(75\sqrt{3} + \frac{75}{\sqrt{3}} \right) \quad [\text{Using (i) and (ii)}]$$

$$\Rightarrow AB = \left(\frac{225 + 75}{\sqrt{3}} \right) = \frac{300}{\sqrt{3}}$$

$$100\sqrt{3} = 100 \times 1.73 \Rightarrow AB = 173 \text{ m}$$

Hence, the distance between the two men is 173 m.

17. Let CE be the 8 m tall building and AD be the multistoried building of height x m.

Let $BC = DE = y$ m, be the distance between the two buildings.

